

MATHEMATICS MARKING SCHEME

1.	$\frac{1}{2}x \frac{7}{2} + \frac{3}{2}\left(\frac{11}{6}\right)$ $\frac{7}{4} + \frac{33}{12} = \frac{55}{12}$ $\frac{3}{4}x \frac{5}{2} \div \frac{1}{4} = \frac{60}{8}$ $\frac{55}{12}x \frac{8}{60} = \frac{11}{18}$	<span style="border: 1px solid black; padding: 2px;">M1</span> <span style="border: 1px solid black; padding: 2px;">M1</span> <span style="border: 1px solid black; padding: 2px;">A1</span>
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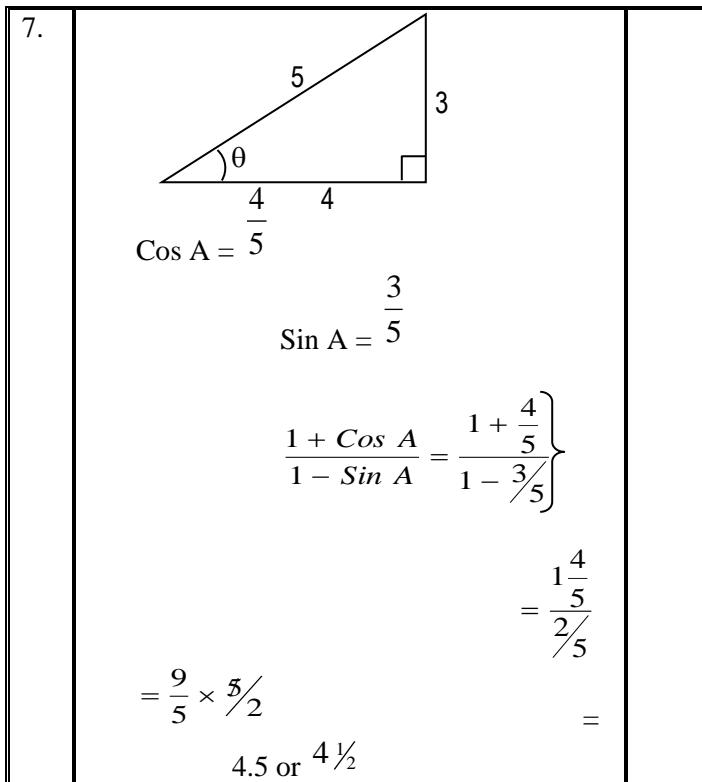
2.	$\frac{3x^2 - 3xy - xy + y^2}{(3x - y)(3x + y)}$ $\frac{(3x - y)(x - y)}{(3x - y)(3x + y)}$ $= \frac{x - y}{3x + y}$	<span style="border: 1px solid black; padding: 2px;">M1</span> <span style="border: 1px solid black; padding: 2px;">M1</span> <span style="border: 1px solid black; padding: 2px;">A1</span>
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3.	$\begin{array}{c cc cc c} 2 & 12 & 18 & 24 & 36 \\ 3 & 6 & 9 & 12 & 18 \\ \hline & 2 & 3 & 4 & 6 \\ & & & & \\ & = 2 \times 3 & & & \\ & = 6 & & & \end{array}$	<span style="border: 1px solid black; padding: 2px;">M1</span> <span style="border: 1px solid black; padding: 2px;">A1</span>
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4.	(i)      19,171,311      M1  (ii)     100,000      A1
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5.	$  \begin{aligned}  & 5 \times \frac{1}{(2.93 \times 10)^2} = 5 \times \frac{1}{8.585 \times 10^2} = 5 \times 0.116 \times 10^{-2} - 8.3780 \\  & = 58.35 - 8.378 \\  & = 49.97  \end{aligned}  $	M1 M1 A1
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6.	$  \begin{aligned}  L_1 \Rightarrow x \geq 0 \\  L_2 \Rightarrow \text{Grad} = \frac{-1}{2} \\  \frac{y - 0}{x - 6} = -\frac{1}{2} \\  2y = -x + 6 \\  L_2 \Rightarrow 2y \leq -x + 6 \\  L_3 \Rightarrow \text{Grad} = 1 \\  \frac{y - 0}{x - 2} = 1 \Rightarrow y = x - 2 \\  y \geq x - 2  \end{aligned}  $	B1 B1 B1
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8.	$  \begin{aligned}  3^{\chi-2} &= 3^{2\chi-1} \\  \chi - 2 &= 2\chi - 1 \\  \chi &= -1  \end{aligned}  $	M1 M1 A1
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9.	$1000\chi = 9.009009$ <hr/> $\chi = \frac{0.009009}{999}$ $\chi = \frac{9}{999}$ $= \frac{1}{111}$	M1 A1
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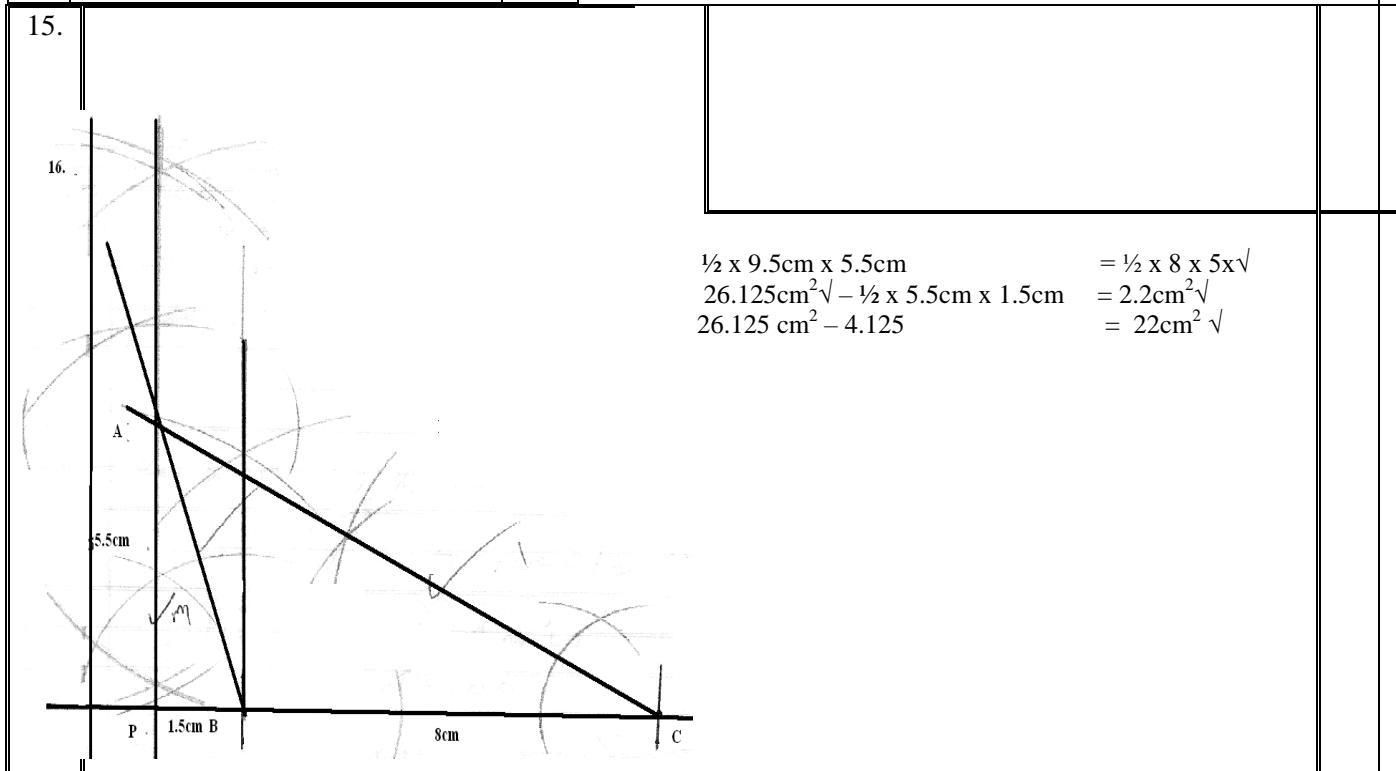
10.	<table style="margin-left: auto; margin-right: auto; border-collapse: collapse;"> <thead> <tr> <th style="text-align: center; border-bottom: 1px solid black;">No</th> <th style="text-align: center; border-bottom: 1px solid black;">Log</th> </tr> </thead> <tbody> <tr> <td style="text-align: right; padding-right: 10px;">47.81</td> <td style="text-align: right; padding-right: 10px;">1.6795</td> </tr> <tr> <td style="text-align: right; padding-right: 10px;">0.7499</td> <td></td> </tr> <tr> <td></td> <td style="text-align: right; padding-right: 10px;">T.8750 +</td> </tr> <tr> <td></td> <td style="text-align: right; padding-right: 10px;">1.5545</td> </tr> <tr> <td style="text-align: right; padding-right: 10px;">823</td> <td style="text-align: right; padding-right: 10px;">2.9154</td> </tr> <tr> <td style="text-align: right; padding-right: 10px;">72.46</td> <td style="text-align: right; padding-right: 10px;">1.8601+</td> </tr> <tr> <td></td> <td style="text-align: right; padding-right: 10px;">4.7755</td> </tr> <tr> <td></td> <td style="text-align: right; padding-right: 10px;">2</td> </tr> <tr> <td></td> <td style="text-align: right; padding-right: 10px;">2.3878</td> </tr> <tr> <td style="text-align: right; padding-right: 10px;">1.468 x 10<sup>-1</sup></td> <td style="text-align: right; padding-right: 10px;">T.1667</td> </tr> <tr> <td></td> <td style="text-align: right; padding-right: 10px;">= 0.1468</td> </tr> </tbody> </table>	No	Log	47.81	1.6795	0.7499			T.8750 +		1.5545	823	2.9154	72.46	1.8601+		4.7755		2		2.3878	1.468 x 10 <sup>-1</sup>	T.1667		= 0.1468	M1 M1 M1 A1
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11.	<p>Let table be x      Chairs will be <math>(x + 10)</math></p> $\left(\frac{3}{100} \times 600\right)(x + 10)$ $+ \left(\frac{4}{100} \times 1500\right)x = 7200$ $18x + 180 + 60x = 7200$ $78x = 7020$ $x = 90$ <p><math>\therefore</math> chairs = 100      Tables = 90</p>	M1 M1 M1 A1
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12.	$\angle AFD = 180^\circ - (30^\circ + 63^\circ)$ $= 87^\circ$	B3
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13.	Cross section Area $= \left( \frac{22}{7} \times 3.5 \times 3.5 \right) + (2 \times 7)$ $= 38.5 + 14 = 52.5$ Volume = $52.5 \times 300$ $= 15750 \text{ cm}^3$ Mass = $15750 \times 8.87$ $= 139702.5 \text{ g}$ $= 139.7 \text{ kg}$	M1 M1 A1
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14.	$x = ti + 2j$ $y = 2i + 3j$ $z = 3i + 4j$ $xy = \begin{pmatrix} 2 & -t \\ 3 & -2 \end{pmatrix} = \begin{pmatrix} 2-t \\ 1 \end{pmatrix}$ $y - z = \begin{pmatrix} 3 & -2 \\ 4 & -3 \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$ collinear points $K \begin{pmatrix} 2-t \\ 1 \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$ $k(2-t) = 1 \Rightarrow K = 1$ $t = 1$	M1 B1 A1
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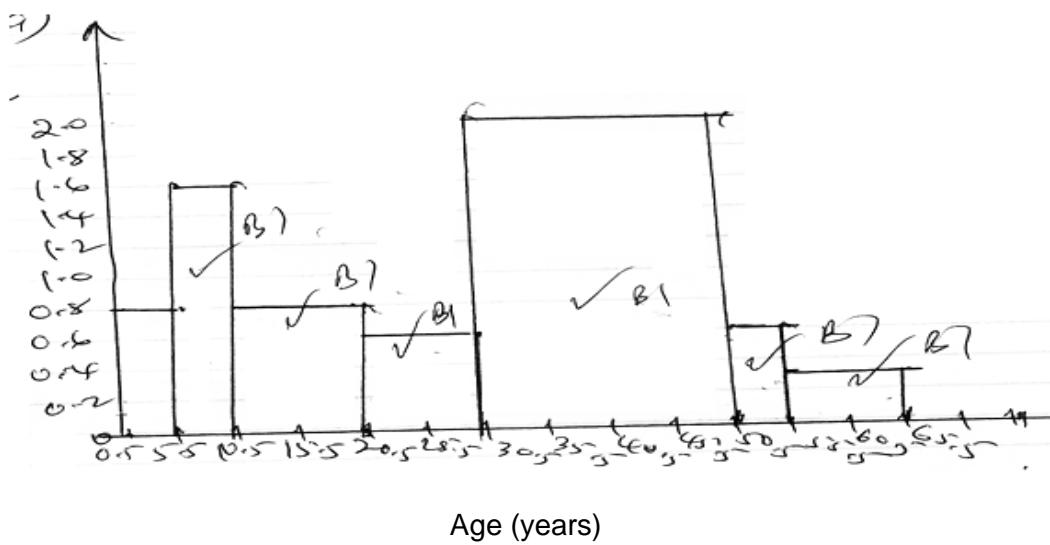


16.	(a) 19.5250 Chinese Yuan into Kenya shillings  = $195250 \times 12.34 = 2409385$	B
	(b) Balance  = $2409385 - 1258000$	M
	= 1151385	M
	Balance in S.A. Rand  = $\frac{1151385}{11.37}$	A
	= 101265	4

## SECTION II

17	(a) Let the constant amount be x  Jane - $(\frac{3}{8}x) / =$ Jepchoge's - $\frac{2}{5}(\frac{5}{8}x) / =$ = $\frac{1}{4}x / =$ Remaining $\frac{3}{5}x - 18,000$ $x = 48,000 / =$  Therefore the original amount is 48,000.  (b) Jepchoge received $(\frac{1}{4}x 48,000)$ = 12,000/  (c) Business maintenance $= (\frac{1}{3}x 12,000)$ = 4,000/ Balance = 8,000/  Ratios: Jane = $(\frac{3}{8}x 48,000)$ = Kshs. 18,000/ Jepchoge - $(\frac{1}{4}x 48,000) / =$ = Kshs. 12,000/ Chepkemboi - $(\frac{1}{3}x 18,000) / =$ = Kshs. 6,000/ Ratio: 18,000 : 12,000 : 6,000 3 : 2 : 1 Jane got $\frac{3}{6} \times 8,000 + 18,000$ = Kshs. 22,000/ Jepchoge got $\frac{2}{6} \times 8,000$ = Kshs. 2,677/ Chepkemboi got $\frac{1}{6} \times 8,000 + 18,000$ = Kshs. 1,337/	M1  M1 A1  M1  M1  M1  M1  M1  M1  A1  B1  B1  B1
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18



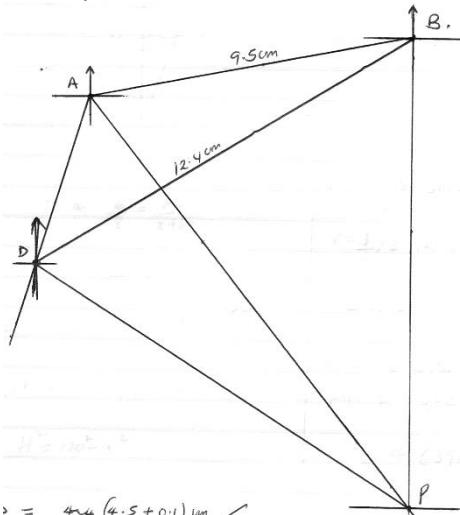
(b)

Class	x	f	$fx$
1 - 5	3	4	12
6 - 10	8	8	64
11 - 20	15.5	8	124
21 - 30	25.5	6	153
31 - 50	40.5	40	1620
51 - 55	53	3	159
56 - 65	60.5	<u>3</u>	<u>181.5</u>
		<u>72</u>	<u>2313.5</u>

$$\begin{aligned} \text{Mean} &= \frac{\sum fx}{\sum f} \\ &= \frac{2313.5}{72} \\ &= 32.13 \end{aligned}$$

19.

1cm rep. 10km



$$(i) \quad AD = (4.5 + 0.1)\text{cm}\sqrt{}$$

$$= (450 + 0.1)\text{km}$$

$$(ii) \quad \text{Bearing of D from B}$$

$$= 240 + 0.10 \sqrt{}$$

$$(iii) \quad \text{Bearing of P from D}$$

$$= 1200 + 0.1 \sqrt{}$$

$$(iv) \quad \text{Distance P to D}$$

$$= 13.6\text{cm} \times 10$$

$$= 136\text{km} + 0.1\sqrt{}$$

21.

a) Length PQ

$$\sin 35^\circ = \frac{x}{8} \Rightarrow x = 8 \sin 35^\circ$$

$$PQ = 2(8 \sin 35^\circ) = 9.18\text{cm}$$

M1

A1

b)  $\sin 20^\circ = \frac{4.5886}{PB}$ 

$$PB = \frac{4.5886}{\sin 20^\circ} = 13.42 \text{ cm}$$

M1

c) Minor segment circle centre A

$$= \frac{70}{360} \times \frac{22}{7} \times 8x8 - \frac{1}{2} \times 8^2 \sin 70^\circ$$

A1

$$= 39.11 - 30.07$$

M1

$$= 9.04\text{cm}^2$$

d) Area of segment centre B

$$= \left( \frac{40}{360} \times \frac{22}{7} \times 13.42 \times 13.42 \right) - \left( \frac{1}{2} \times 13.42^2 \sin 40^\circ \right)$$

M1

A1

$$= 62.89 - 57.88$$

M1

$$= 5.01 \text{ cm}^2$$

Area of shaded region

$$= (30.07 + 57.88) - (5.01 + 9.04)$$

A1

$$= 87.95 - 14.05$$

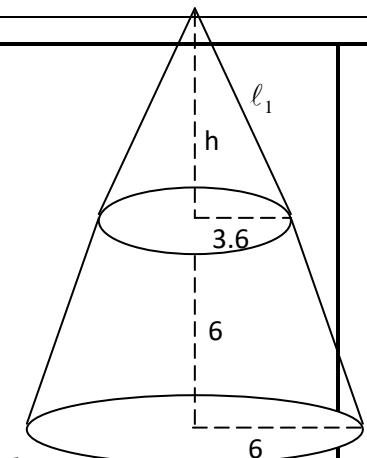
M1

$$= 73.90\text{cm}^2$$

A1

20

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$$\frac{6}{3.6} = \frac{6+h}{h}$$

$$6h = 3.6 \times 6 + 3.6h$$

$$h = 3.6 + 0.6h$$

$$0.4h = 3.6$$

$$h = \frac{3.6}{0.4} = \frac{36}{4} \sim 9\text{cm}$$

$$l_1^2 = 9^2 + 3.6^2$$

M1

M1

$$l_1^2 = 81 + 12.96 = 93.96$$

$$l_1 = 9.69$$

$$L^2 = 6^2 + 15^2$$

$$L = \sqrt{36 + 225}$$

$$L = \sqrt{261} = 16.12$$

S.A of frustum =  $\left( \frac{22}{7} \times 6 \times 16.12 - \frac{22}{7} \times 3.6 \times 9.69 \right)$

M1

A1

$$+ \frac{22}{7} \times 3.6 \times 3.6 \Big)$$

$$= 303.98 - 109.64 + 40.73$$

$$= 235.07$$

S.A of cylinder =  $2\pi Rh + \pi R^2$

M1

$$= 377.14 + 113.14$$

(S.A of cylinder)

$$= 490.28$$

A1

$$\text{Total S.A} = 490.28 + 235.07$$

$$= 725.35\text{cm}^2$$

M1

(b) Volume of frustum =

$$\left( \frac{1}{3} \times 6 \times 15 \times \frac{22}{7} \times 6 - \frac{1}{3} \times \frac{22}{7} \times 3.6 \times 3.6 \times 9 \right)$$

$$= 565.71 - 122.19$$

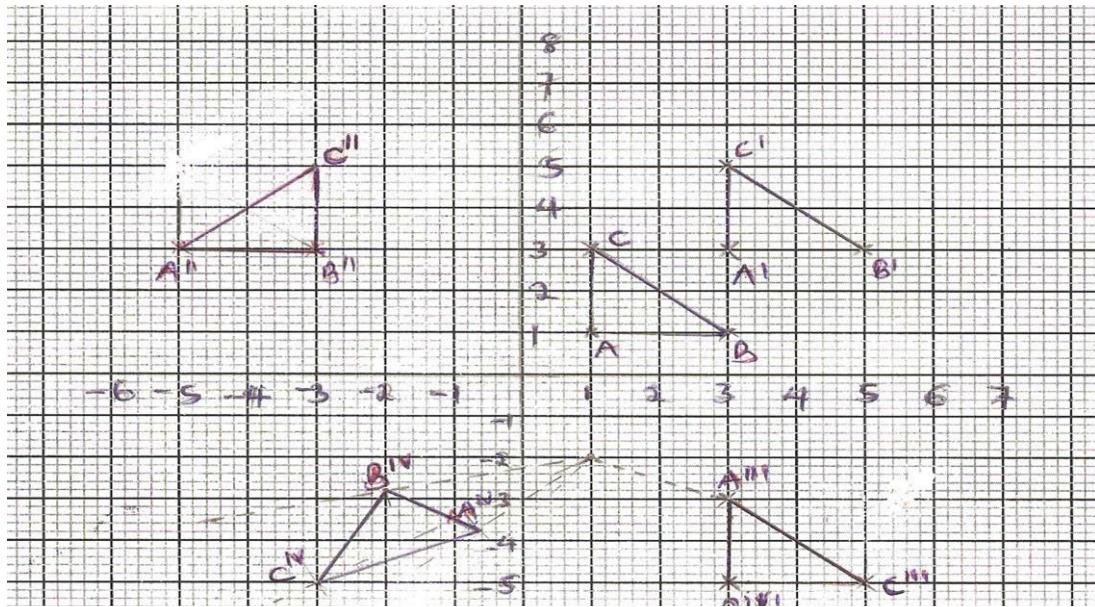
M1

$$= 443.52\text{cm}^3$$

M1

	Volume of cylinder $\Pi^2h$ $\frac{22}{7} \times 6 \times 6 \times 10$ $= 1131.43$ Total volume = $443.52 + 1131.43$ M1 $= 1574.95$ A1	

22.

Triangles that are congruent  $A^1B^1C^1$  and  $A^{111}B^{111}C^{111}$ 

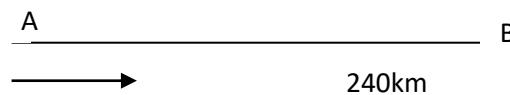
$$A^1 = \begin{pmatrix} 1 \\ 1 \end{pmatrix} + \begin{pmatrix} 2 \\ 2 \end{pmatrix} = \begin{pmatrix} 3 \\ 3 \end{pmatrix}$$

$$B^1 = \begin{pmatrix} 3 \\ 1 \end{pmatrix} + \begin{pmatrix} 2 \\ 2 \end{pmatrix} = \begin{pmatrix} 5 \\ 3 \end{pmatrix}$$

$$C^1 = \begin{pmatrix} 1 \\ 3 \end{pmatrix} + \begin{pmatrix} 2 \\ 2 \end{pmatrix} = \begin{pmatrix} 3 \\ 5 \end{pmatrix}$$

23.

(a) 90km/h



120km/h

After 20 min

$$\frac{20}{60} \times 120 = 40\text{km}$$

$$\frac{20}{60} \times 90 = 30\text{km}$$

$$\frac{30}{60} \times 90 = 45\text{km}$$

$$45\text{km} - 10\text{ km} = 35\text{km}$$

$$\text{R. speed } (120 - 90) \text{ km/h} = 30\text{km/h}$$

$$\text{Time taken } \frac{35}{60} = 1\frac{1}{6} \text{ hrs}$$

$$40 + \frac{35}{30} \times 120 = 140 + 40 = 180\text{km}$$

$$(b) 0850 + 0150 \text{ hrs} = 1000\text{hrs}$$

$$c) \frac{240}{90} = 2\frac{2}{3} \text{ hrs}$$

2 hrs 40 min

$$0800 \text{ hrs} + 0240 \text{ hrs} = 1040 \text{ hrs} \\ = 10.40 \text{ AM}$$

M1

M1

M1

M1

M1

A1

B1

M1

M1

A1

24.

a.  $7y = 3x - 30$

$$Y = \underline{3x} - \underline{30}$$

7      7

M1

$Y$  intercept = -30

7

$X$  intercept = 10

A is (10, 0)

M1

Based on line  $y = -x$

$$Y = \underline{3x} - \underline{30} = \underline{3(-y)} - \underline{30}$$

7      7      7      7

$$Y = -3y - 30$$

M1

7      7

$$\frac{10y}{7} = \frac{-30}{7}$$

$$Y = -3$$

$$\therefore x = 3$$

A1

$$B(3, -3)$$

b.	$\begin{aligned} 8-k &= -3 \\ k-3 & \\ 8-k &= -3k + 9 \\ 2k &= 1 \\ \therefore k &= \frac{1}{2} \\ \text{Taking a general point } (x, y) \\ Y-8 &= -3x + \frac{3}{2} \\ 3x+y &= 9 \frac{1}{2} \text{ or } 6x+2x+2y = 19 \end{aligned}$	M1 M1 A1
c.	$\begin{array}{rcl} \underline{6+2} & \underline{1+3} & = (4,2) \\ 2 & 2 & \\ \underline{1-3} & \times u_2 & = -1 \quad (M_2 = 2) \\ 6-2 & & \\ Y-2 & = 2 & \\ X-4 & & \\ \therefore 2x-y & = 6 & \end{array}$	M1 M1 A1

